Frugal Paradigm Completion

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Abstract

Lexica distinguishing all morphologically related forms of each lexeme are crucial to many language technologies, yet building them is expensive. We propose a *frugal paradigm completion* approach that predicts all related forms in a morphological paradigm from as few manually provided forms as possible. It induces typological information during training which it uses to determine the best sources at test time. We evaluate our languageagnostic approach on 7 diverse languages. Compared to popular alternative approaches, ours reduces manual labor by 16-63% and is the most robust to typological variation.

1 Introduction

From syntactic parsing (Seeker and Kuhn, 2013) to text-to-speech (Zen et al., 2016; Wan et al., 2019), many linguistic technologies rely on accurate lexica decorated with morphological information. Yet, building such lexica requires much human effort (Buckwalter, 2002; Tadić and Fulgosi, 2003; Forsberg et al., 2006; Sagot, 2010; Eskander et al., 2013). We present a language-agnostic method for minimizing the manual labor required to add new paradigms to an existing lexicon.

Formally, let each lexicon entry, or realization, be a triple (P, C, f). P marks membership in some paradigm \mathbb{P} of morphologically related words, C defines a cell in \mathbb{P} as a bundle of morphosyntactic features, and f is the form realizing C in \mathbb{P} . Hence, paradigm SING can be expressed (in the UniMorph schema (Kirov et al., 2018)) as a set of realizations: {(SING, NFIN, *sing*), (SING, 3.SG.PRES, *sings*), ... }.

For each paradigm to be added to the lexicon, e.g., \mathbb{FLY} , we aim to select as few sources as possible to be manually realized, e.g., {(FLY, NFIN, *fly*), (FLY, PST, *flew*)} such that the forms realizing the remaining cells can be predicted, e.g., *flies*, *flying, flown.* Here, sources are manually provided realizations. Targets are realizations whose forms must be predicted from sources. Our work differs from traditional paradigm completion (Durrett and DeNero, 2013) in that sources are not given, but strategically selected.

Paradigm completion from one source is typically non-deterministic due to multiple inflection classes realizing different exponents in some cells, e.g., suffixing +ed generates the past tense for WALK, but not for SING or FLY which are members of different classes. Hence, many works discuss paradigm completion in the context of (implicit) inflection class disambiguation (Ackerman et al., 2009; Montermini and Bonami, 2013; Beniamine et al., 2018). Finkel and Stump (2007) propose three approaches to select the fewest sources required to deterministically identify class. Yet, neural sequence models can often complete paradigms accurately from less sources without fully disambiguating inflection class (Kann and Schütze, 2016; Aharoni and Goldberg, 2017; Wu and Cotterell, 2019). For an overview of the application of neural sequence models to morphological theory, we point the reader to Elsner et al. (2019).

We propose Frugal Paradigm Completion (FPC), inspired by work on inflection class disambiguation and neural sequence modeling. We train a *source selection agent* (SSA) to induce typological knowledge regarding the distribution of complexity in paradigms and use this to request informative source cells to be realized by an *oracle*. Sources are fed to a *predictor* to generate target forms. For each paradigm, SSA iteratively requests sources until the oracle confirms all cells have been realized correctly.

We introduce a novel metric, *auto-rate*, to quantify the manual labour (performed by the oracle) needed to complete each paradigm. This metric demonstrates that FPC reduces labor by 63% over predicting targets from lemmata, and 47% over predicting them from the smallest set of sources that fully disambiguates inflection class. We propose a new typology for discussing the organization of complexity in paradigms which helps explain why strategies perform better or worse on certain languages while FPC, being sensitive to typological variation, performs robustly.

After discussing related paradigm completion approaches in Section 2, we describe FPC in Section 3. Section 4 covers all data and experimental set up details. We discuss results in Section 5 and analyze FPC's behavior in Section 6.

2 Paradigm Completion Approaches

Here we discuss several paradigm completion approaches related to FPC, though not necessarily proposed for the same task setup under the same assumptions.

Lemma-based Paradigm Completion The standard paradigm completion approach does not select sources, but assumes one source: the lemma (Dreyer and Eisner, 2011), whose distinction is ultimately arbitrary. Yet many have shown that more informative sources can be chosen (Finkel and Stump, 2007; Cotterell et al., 2017b; Kann and Schütze, 2018).

Most Informative Source For each target form to be predicted, Kann and Schütze (2018) select the source most likely to predict that form. Yet, unlike FPC, they do not attempt to minimize the number of unique sources that must be manually realized.

Static Principal Parts To minimize sources required to fully disambiguate inflection class, Finkel and Stump (2007); Stump and Finkel (2013) propose three approaches: *static, dynamic,* and *adaptive*. In the static approach, the same sources—referred to as principal parts in a much older pedagogical tradition (Grinstead, 1916; Ahern, 1990)—must be used for every paradigm. Cotterell et al. (2017b) train a model on static sources and attain near 100% accuracy in Latin verb paradigm completion. However, they do not consider that one paradigm may require fewer sources than another, nor that paradigm completion may require fewer sources than inflection class disambiguation.

Dynamic Principal Parts Finkel and Stump (2007)'s dynamic approach selects a minimal set of sources necessary to fully disambiguate inflection class which can be unique to that inflection class. While efficient, this is impractical in that it requires oracular knowledge of class prior to seeing any forms.

Adaptive Principal Parts Finkel and Stump (2007)'s adaptive approach, like our FPC method, chooses the same first source cell for each paradigm \mathbb{P} . Subsequent sources are selected conditional on the set of inflection classes \mathbb{P} could belong to given the sources realized so far. Hence, the number of sources required per paradigm is upper bounded by the static approach and lower bounded by the dynamic.

Our FPC approach is a neural update, inspired by their adaptive approach. While their implementation tracks viable inflection classes explicitly with rules operating on oracularly segmented affixes, we use sequence models operating on whole words to remove reliance on oracular segmentation and leverage stem-internal phonology known to correlate with inflection class (Aronoff, 1992; Dressler and Thornton, 1996; Dawdy-Hesterberg and Pierrehumbert, 2014).

3 Frugal Paradigm Completion

This section and Figure 1 describe the interactions of the three FPC components. In general, the predictor takes a source cell and its realizing form as input, e.g., 3.SG.PRES: sings, or cell 2: form 2 in the figure. The predictor is composed of as many sub-predictors as there are cells in the paradigm, each of which is trained to predict the entire paradigm from one source cell's realization. Cell 2 in the paradigm is grayed out in the figure, as this was provided as input so it does not have to be predicted. The predicted paradigm is evaluated by the oracle. If there are no errors, we are done. Otherwise, based on previous sources, SSA chooses a new cell to be realized by the oracle and gives it to the predictor as the next source. Because cell 3 is chosen in the figure, sub-predictor 3 will be used to predict the paradigm going forward, and cells 2 and 3 will both be grayed out. The process continues like this until all cells have been correctly predicted by at least one sub-predictor.

Crucially, during inference, each test paradigm is empty, i.e., no realization has been seen during training and no source is available to inflect



Figure 1: Schematic representation of the flow of Frugal Paradigm Completion at inference time.

from *a-priori*. Our human-in-the-loop setup aims to minimize the number of sources which the SSA must request from the oracle to predict the remaining paradigm slots correctly. Because we use as many sources as are necessary to reach 100% accuracy in predicting the remaining slots, accuracy is not a meaningful metric for the FPC. We discuss alternative metrics in Section 4.3.

3.1 Predictor

The predictor outputs a target form given its cell, a source form and the source form's cell as input. To train the predictor, for each possible source cell, we train a sub-predictor to predict every possible target form in every paradigm in the training data given the realization of that source cell in that paradigm. Details of all sequence model architectures are provided in Section 4.

3.2 Source Selection Agent

SSA's choice of a cell for a given paradigm depends on all previously selected cells for that paradigm and their corresponding forms. This allows SSA to learn, e.g., that given a previous English PST source, PST.PTCP should only be requested as a subsequent source if the PST form did not take the regular *-ed* suffix. Otherwise, PST.PTCP is likely to be regular and unlikely to contribute new information.

To induce such knowledge, we train SSA on an oracle policy of ideal source selections extracted from the train set (Ross et al., 2011; Ross and Bagnell, 2014; Welleck et al., 2019).¹ To extract the oracle policy, we divide the training lexicon into two folds and train one predictor on each, allowing us to cross-validate each predictor on its held out

fold. For each training paradigm, we test which target forms can be correctly predicted by which source cells' sub-predictors. As shown for SING in Figure 2, we use this information to extract minimum set covers, i.e., the fewest source cells such that the union of the subsets they predict correctly covers the entire paradigm. These covers constitute the oracle policy used to train SSA.

The minimum set cover problem is NPcomplete (Lund and Yannakakis, 1994; Kuhn et al., 2005), but we approximate it in $O(log_e|\mathbb{P}|)$ by iteratively selecting the cell whose subset most enlarges the union. We break ties by averaging predictiveness (Equation 1) over both folds, where fold F contains |F| paradigms; \mathbb{P}_m , $|\mathbb{P}_m|$ cells; and Acc(\mathbb{P}_m , C_{trg}, C_{src}) returns 1 if using C_{src}'s realization as a source correctly predicts the form realizing cell C_{trg} in paradigm \mathbb{P}_m .

$$predictiveness(C_{src}, F) = \frac{\sum_{m=1}^{|F|} \sum_{j=1}^{|\mathbb{P}_m|} Acc(\mathbb{P}_m, C_j, C_{src})}{\sum_{m=1}^{|F|} |\mathbb{P}_m|}$$
(1)

At this stage, paradigm covers are dynamic in that no single cell need be shared by all covers. Yet, when selecting the first source, SSA has no previous sources to condition on, making it impossible to predict the first cell. Thus, we get adaptive minimum set covers by designating the *start cell* to be that which occurs in the most dynamic covers. Then we re-approximate all covers such that each includes this cell.² Finally, we rank cells within each cover by the total number of covers in which they appear. For each cell in each cover, we train SSA to predict said cell from all higher

¹While we borrow the term *oracle policy* from Imitation Learning (Ross et al., 2011; Ross and Bagnell, 2014; Welleck et al., 2019), we mimic the oracle policy with simple sequence learning. Our analysis suggests even this may be more machinery than necessary.

²We train and test on a single part-of-speech for each language, so each paradigm *should* contain the start cell. For defective paradigms lacking said cell, we back off to the most frequent cell that exists in the paradigm.

	NFIN=sing \\NFIN=sing	NFIN=sing
	3.SG.PRES=sings 3.SG.PRES=sings	3.SG.PRES=sings
Targets predicted correctly	PRES.PTCP=singing PRES.PTCP=singing	PRES.PTCP=singing
		/ PST=sang
		PST.PTCP=sung PST.PTCP=sung
Given	NFIN=sing / 3.SG.PRES=sings	PRES.PTCP=singing` PST=sang / PST.PTCP=sung

Figure 2: Example minimum set cover for SING is {NFIN, PST}.

ranked cells and their realizing forms (holding out 2% of them for development).

3.3 Oracle

The oracle represents a human-in-the-loop during inference, providing requested source realizations to the predictor and informing SSA when a paradigm is complete and accurate (Figure 1). In our implementation, the oracle does not specify which individual predictions are incorrect, but it thus must resolve any discrepancies when two sub-predictors disagree after the fact. We do not attempt to model the additional cost this incurs, as it is unclear how to combine it with the presumably more expensive cost of correcting errors, which we model instead. This is worth re-visiting in future work.

4 Experimental Details

We evaluate 4 paradigm completion approaches on 7 languages. Here we discuss implementation, data and evaluation details.

4.1 Prediction Architecture

All sequence models in all implementations of any paradigm completion approach use the transformer architecture (Vaswani et al., 2017). Here we describe the formatting of input and outputs as well as our hyperparameters so that our experiments can be reproduced.

Input and Output Formats Following Kann and Schütze (2016), input sequences combine characters and morphosyntactic features. The following is a sample input and output for a single source FPC sub-predictor specializing in the cell NFIN:

Input: *f l y* out_V.PTCP out_PST Output: *f l o w n*

For any inflected-form-predicting sequence model whose input is not limited to realizations of

a single cell—as in, e.g., the static principal parts approach—source cell features are prepended to the input as such:

Input: in_NFIN *f l y* out_V.PTCP out_PST Output: *f l o w n*

For multi-source sequence models, the features of each source are inserted into the input and the target features are listed after the first source. We experimented with several different multisource representations and the transformer performed fairly similarly with all of them.

```
Input: in_NFIN f l y out_V.PTCP out_PST
in_PST f l e w
Output: f l o w n
```

The FPC's SSA predicts not a form, but a cell, conditional on any previously realized sources. To predict the first source, it is given nothing and will thus deterministically select the best starting cell as determined by the oracle policy. To predict the third source, it conditions on the first two realizations. The following exemplifies SSA inputs and outputs when predicting the second source for paradigm \mathbb{FLY} :

```
Input: in_NFIN f l y
Output: in_V.PTCP in_PST
```

Wu et al. (2018) and others have achieved improvements by embedding morphosyntactic features separately and concatenating them to the encoder output prior to feeding it to the decoder. Our error analysis, however, suggests transformers handle Kann and Schütze (2016)-style input well. More sophisticated feature handling may not be necessary, but should be investigated in future work.

Hyperparameters We train all transformer models for 100 epochs in batches of 64 with 0.1

		Train	Dev	Test
Arabic	paradigms	1006	100	100
nouns	instances	24160	2260	2352
German	paradigms	1031	100	100
verbs	instances	27762	2690	2692
English	paradigms	2908	200	201
verbs	instances	14522	1000	1001
Russian	paradigms	3289	100	100
nouns	instances	37423	1133	1137
Latin	paradigms	1630	100	100
nouns	instances	19150	1180	1174
Hungarian	paradigms	1405	100	100
nouns	instances	47689	3400	3383
Irish	paradigms	549	100	100
nouns	instances	6460	1197	1195

Table 1: Number of paradigms and instances by split for every language and POS considered.

dropout. The final model is restored from the epoch with the highest dev accuracy. We stop early if there is no improvement for 20 epochs. The only exception is during FPC cross-validation where sub-predictor models are trained for only 50 epochs with early stopping after 5. This is just to reduce computational cost as it is sufficient to induce an oracle policy. The final sub-predictor models however (those used at inference time, not those used to induce the oracle policy), are trained on the full training data set using the full 100 epochs with 20 epochs patience for early stopping. As for transformer-specific hyperparameters, we set N = 4, $d_{model} = 128$, $d_{ff} = 512$, and h = 8, scaling down the hyperparameters recommended for machine translation (Vaswani et al., 2017) as our task is less expensive (Aharoni and Goldberg, 2017; Wu et al., 2018).

4.2 Data Preparation

For every language and part of speech (POS) considered, we extract train, dev and test lexica from UniMorph (Kirov et al., 2018). Each split contains full paradigms, though the cells realized in each may vary due to defectiveness (Corbett, 2005; Sims, 2015). We filter many gold errors by removing paradigms for which no realization can be attested in actual text. We use Universal Dependencies (UD) (Nivre et al., 2016) to check for attestations. We also filter overabundant realizations (multiple forms realizing one cell), keeping only the most frequent form, as attested in UD. Some languages allow for overabundance (Thornton, 2010, 2011), but in UniMorph, this often indicates a gold error.

We randomly divide paradigms into splits such that train is maximally large and dev and test contain at least 100 paradigms and 1,000 realizations. Exact quantities are displayed in Table 1. Arabic, German, English, and Russian were used for development, while Irish, Hungarian, and Latin were only evaluated after fixing hyperparameters. The languages considered represent 3 families and 4 diverse Indo-European branches. They exhibit multiple *non-canonical* behaviors (Corbett, 2005) and present diverse challenges from nonconcatenative morphology to complex inflection class systems.

4.3 Evaluation

Paradigm completion is usually evaluated via exact match *accuracy* on held out target forms (Cotterell et al., 2016, 2017a, 2018; McCarthy et al., 2019). Yet theoretical works often focus on the sources required to unambiguously complete a paradigm given some implicit knowledge of viable inflection classes (Finkel and Stump, 2007; Ackerman and Malouf, 2013). To bridge these traditions, we propose *auto-rate*:

$$auto-rate = \frac{\sum_{i=1}^{n} auto(\mathbb{P}_i)}{\sum_{i=1}^{n} |\mathbb{P}_i|},$$
 (2)

where $auto(\mathbb{P})$ denotes the number of realizations correctly predicted while not having been provided as sources for paradigm \mathbb{P} by the oracle.

Intuitively, auto-rate is like accuracy but it counts oracularly provided sources as additional errors since both errors and sources require labor, i.e., sources require manual input and errors, post-correction. We also report *manual cells per paradigm*, i.e., sources plus errors. Of course, FPC resolves all errors eventually, but other systems can make errors requiring post-correction.

4.4 Baselines

We compare the FPC method to three baselines. One is a variant of FPC using a *random* SSA. This allows us to distinguish the benefit of a smart SSA from that of simply receiving additional feedback from an oracle in the loop. Each time a source must be selected, random SSA chooses randomly without replacement. Its performance is averaged over two runs. The *lemma* approach baseline predicts all paradigm forms from one designated source: the lemma. Finally, for the *static* approach baseline, we consider two *static* approach implementations. The single-source implementation predicts each target from the source that is, in theory, its best predictor (Kann and Schütze, 2018). The multi-source implementation concatenates these sources, predicting each target from the concatenated input. Results are nearly identical for either implementation; reported results are single-source (with the exception of Latin, to be explained presently).

For some languages, there is little theoretical or pedagogical literature to help identify the best sources for the static approach. Our single-source static approach for Arabic nouns predicts singular and dual forms from SG;NDEF;NOM and plurals from PL;NDEF;NOM. In theory, any nonplural plus any plural should be sufficient (Brustad et al., 2005; Habash, 2010). For German verbs, we predict present and imperative forms from NFIN and past forms from IND;PST;1SG. We predict English present forms from NFIN; PST and V.PTCP;PST predict themselves. For Russian nouns, Zaliznyak (1980) argues for five sources, yet Parker (2016) demonstrates that three are usually sufficient. We follow the latter, predicting all nominative or accusative forms from ACC;SG, all other singulars from INS;SG, and all other plurals from GEN;PL. In preliminary experiments, we found this to match the accuracy of the five source approach, thus achieving a higher auto-rate. For Latin, we could not evaluate a single-source static implementation as it is unclear which source cell best predicts each target. The multi-source static approach for Latin nouns predicts all forms from NOM;SG and GEN;SG (Whitaker, 2016). For Irish and Hungarian, we do not evaluate a static approach as we lack the requisite linguistic knowledge to determine the best sources.

5 Results and Discussion

As shown in Table 2, FPC always ties or beats the next best approach, while the next best approach varies by language. On average, FPC reduces labor by 63% over the lemma approach, 47% over static, 16% over random agent, and 13% over the next best approach. Its success is mainly due to (1)

	Ac	curacy	Aut	o-rate	Мс	epp
	Dev	Test	Dev	Test	Dev	Test
		Arabic	nouns			
Lemma	62.0	58.8	59.3	56.5	9.6	10.7
Static	95.9	99.4	89.5	93.1	2.9	2.1
Random Ag.			90.2	90.9	2.2	2.2
FPC			90.2	93.6	2.2	1.5
		Germa	n verbs			
Lemma	87.6	89.0	84.1	85.8	4.3	4.0
Static	94.1	96.4	86.7	88.9	3.6	3.0
Random Ag.			90.0	92.1	2.4	1.9
FPC			91.8	92.5	2.0	1.8
		English	ı verbs			
Lemma	96.5	94.0	76.7	74.2	1.2	1.3
Static	99.7	98.4	39.7	38.4	3.0	3.0
Random Ag.			76.0	73.3	1.2	1.4
FPC			77.3	74.3	1.1	1.3
		Russiar	n nouns			
Lemma	97.1	95.6	88.3	87.5	1.3	1.5
Static	98.4	98.3	72.6	72.3	3.2	3.2
Random Ag.			86.1	84.3	1.6	1.8
FPC			88.5	89.1	1.3	1.2
		Latin	nouns			
Lemma	65.5	51.6	63.6	49.6	5.1	6.7
Static	97.7	96.8	80.8	79.7	2.3	2.4
Random Ag.			85.9	84.7	1.7	1.8
FPC			89.0	87.8	1.3	1.4
	H	Iungaria	an noun	s		
Lemma	95.6	90.9	92.8	88.0	2.5	4.1
Random Ag.			95.0	94.6	1.7	1.9
FPC			95.5	95.2	1.5	1.6
		Irish I	nouns			
Lemma	63.5	66.9	56.1	59.6	5.4	5.0
Random Ag.			64.9	68.2	4.2	3.8
FPC			72.1	69.6	3.3	3.6

Table 2: Evaluation of paradigm completion approaches with metrics defined in Section 4. We do not report accuracy for FPC or its random agent variant (Random Ag.), as it is trivially 100% (see Section 3). Mcpp stands for *Manual cells per paradigm*.

making predictions from fewer sources than are required for fully disambiguating inflection class and (2) receiving feedback after each source.

Surprisingly, training a sophisticated SSA does not improve much over using a random agent. We argue this is due to an unexpectedly large margin of error in the agent's source selection task. Despite the complexity of source selection strategies required for inflection class disambiguation, FPC uses lexical frequencies to expect regularity and stem-internal clues to anticipate irregular classes, requiring a median of just one source per paradigm for all languages except under-resourced Irish. Furthermore, inspection of the source selection minimum set covers reveals that it is often the case that a paradigm can be completed correctly from any single source. This is surprising in light of the precise strategies required for completely deterministic paradigm completion in Finkel and Stump (2007)'s framework and in light of Albright (2002)'s case for the privileged status of a single form per paradigm, though in our framework with full words and full paradigms for training, it seems that many sources can often serve as *good enough* singleton principal parts. This supports Bonami and Beniamine (2016) proposal of gradient principal part analyses.

6 Analysis

Here, we discuss patterns relating SSA's first and second sources chosen (Figures 3a-b and 4a-b) to the inter-predictability of cells represented by heat maps (3c and 4c). Maps display the average accuracies with which each target (column) can be predicted from each source (row). We analyze specific SSA choices and predictor errors in Arabic and Latin.

The maps (for all languages, see the Appendix) suggest complexity can be distributed within paradigms in systematically distinct ways. Ackerman and Malouf (2013) propose integrative (I-) complexity, using average conditional entropy to describe paradigmatic organization, but this has been criticized for obscuring differences in the predictability of sub-paradigm regions (Cotterell et al., 2019; Elsner et al., 2019). To remedy this, we propose a typology for measuring the extent to which I-complexity is realized via different organizational strategies, which is useful for discussing source selection strategies. Our typology describes paradigms in terms of mutual predictability, the correlation of a map and its transpose, and entropy predictiveness, the negative correlation of cells' average predictiveness (see Equation 1) and average predictability (defined here in comparable terms).

$$predictability(C_{trg}, F) = \frac{\sum_{m=1}^{|F|} \sum_{j=1}^{|\mathbb{P}_m|} Acc(\mathbb{P}_m, C_{trg}, C_j)}{\sum_{m=1}^{|F|} |\mathbb{P}_m|}$$
(3)

Intuitively, a paradigm is mutually predictable if the fact that cell A predicts cell B means that B is likely to predict A. Such paradigms often feature regions of mutually predictable cells (as in 3c), such that an optimal strategy avoids picking multiple sources from one region. For entropy predictive paradigms, if A is generally more difficult to predict than B, A is likely to be a better predictor of the remaining cells (following the information theoretic logic that surprisal is informative (Shannon, 1948; Jaeger, 2010)). For such paradigms, the optimal strategy selects the source which would have been the most difficult target to predict.

Unlike Sims (2020)'s graph-theoretic typology for describing inflection class structure, our typology is a two-dimensional description of how the optimal paradigm completion strategy is affected by underlying class structure. In this sense, our typology is complementary to hers and future work might investigate the relationship between traits in her typology and mutual predictability or entropy predictiveness. Furthermore, our typology might be updated to consider the impact of type frequency (Sims and Parker, 2016) in a framework where distributional data is available.

Figure 5 demonstrates that cross-linguistic variation is vast with respect to our typology, as some languages even exhibit negative entropy predictiveness or mutual predictability. This partly explains why non-FPC approaches perform erratically: if paradigmatic organization varies by language, source selection strategies must be able to adapt to the data.

6.1 Arabic Error Analysis

Arabic nouns are mutually predictable (Figure 5). Any singular or dual form can predict another. Plural forms also predict each other. Yet, in general, plurals are less predictive/able (Figure 3c) due to several inflection classes varying in the plural. The *sound* plurals take suffixes while *broken* plural classes are realized via non-concatenative processes. For example, راکب *rAkb*, *rider* from root r *k b*, takes the broken plural pattern $_A$, becoming rkAb. Yet, having heard only singular realizations, a human might posit a sound plural, i.e., **ikbyrAkbwn*, realizing the more productive exponent.

SSA learns an ideal strategy, requesting a singular source (Figure 3a) and then a plural (3b). Interestingly, 6 of 18 sound feminine plurals (most frequent single class) require multiple sources and 8 of 28 broken plurals do not. Thus, the predictor does not default to regularity, but uses stem-



Figure 3: Arabic analysis. (a) and (b) define how likely each cell is to be a source (white), correctly predicted (gray), or an error (black) after one (a) or two (b) sources. (c) shows the predictiveness/ability of source (rows) and target (columns) cells. Darker cells are less predictive/able.

internal phonology to anticipate irregularity. Most errors made from the first source posit a viable broken plural, just not the right one. In future work, modeling semantics can fix such errors, e.g., knowing that راكب rAkb is animate makes plural * رواكب rwAkb unlikely, as animate nouns seldom take that inflection class.

For future work, we can pre-train on raw corpora to give our model access to such information (Devlin et al., 2019). Indeed Erdmann and Habash (2018) found distributional information to benefit inflectional paradigm clustering in Arabic. Though the benefits should generalize as se-



Figure 4: Latin analysis. (a) and (b) define how likely each cell is to be a source (white), correctly predicted (gray), or an error (black) after one (a) or two (b) sources. (c) shows the predictiveness/ability of source (rows) and target (columns) cells. Darker cells are less predictive/able.

mantics correlates with inflection class in many languages (Wurzel, 1989; Aronoff, 1992; Harris, 1992; Noyer, 1992; Carstairs-McCarthy, 1994; Corbett and Fraser, 2000; Kastner, 2019).

6.2 Latin Error Analysis

Latin is not mutually predictable with moderate entropy predictiveness. SSA's choices are, at first, opaque, but Table 3 shows that ACC;PL narrows the inflection class to variants of one declension. Remaining ambiguity mostly involves 3^{rd} declension nominative and vocative realizations, which can usually be predicted from the pre-



Figure 5: Integrative typology for describing paradigms by the mutual predictability of cells and the predictive power of hard-to-predict cells.

Cell	1^{st}	$2^{nd}\mathbf{M}$	$2^{nd}\mathbf{N}$	3^{rd}	$4^{th}\mathbf{M}$	$4^{th}{\rm N}$
NOM;SG	а	us	um	varies	us	ū
GEN;SG	ae	ī	ī	is	ūs	ūs
DAT;SG	ae	ō	ō	ī	uī	ū
ACC;SG	am	um	um	em	um	ū
ABL;SG	ā	ō	ō	em	ū	ū
VOC;SG		genera	ally mat	ches NO	M;SG	
NOM;PL	ae	ī	а	ēs	ūs	ua
GEN;PL	arum	ōrum	ōrum	um	uum	uum
DAT;PL	is	īs	īs	ibus	ibus	ibus
ACC;PL	as	ōs	а	ēs	ūs	ua
ABL;PL	is	īs	īs	ibus	ibus	ibus
VOC;PL		gener	ally mat	ches NO	M;PL	

Table 3: Plat of the suffixes taken for each Latin nominal declension.

ferred second source cell, VOC;SG. 44 of 100 test paradigms were 3^{rd} declension, which required multiple sources at the highest rate (16 of 44; 2^{nd} masculine declension was next highest at 3 of 15). There was no correlation between declension and second source chosen, yet high auto-rate suggests SSA's choices may not need to condition on previously realized source forms, but only their cells.

While 77 of 100 paradigms were completed from a single source, we found paradigms requiring three sources that might be completable from two using a multi-source FPC implementation. For example, *gregēs*, *flocks* realizes $\mathbb{GREX.ACC;PL}$, but the predictor mistakenly posits **gregium* for GEN;PL from this source, guessing the wrong 3^{rd} declension variant. While second source VOC;SG *grex* corrects this, it obscures the underlying stem, as x can be an allophone of g or c. Thus, we still get an error, *grecum. A multi-source predictor could avoid forgetting the underlying allophone g after seeing the second source.³ That said, multi-source FPC is not as simple as multi-source static. Heuristic sampling of training instances based on the oracle policy yields predictors that only attend to one source or make bad predictions when only given one. This is worth exploring further in future work as there is more evidence of paradigms that are difficult to handle without jointly encoding sources in the linguistic literature (Corbett, 2005; Bonami and Beniamine, 2016).

7 Conclusion

We presented Frugal Paradigm Completion, which reduces the labor required to expand a morphological lexicon by 16-63% over competitive approaches across 7 languages. We demonstrated that typologically distinct morphological systems require unique treatment and benefit from our SSA, that learns its strategy from data. We found that inducing this strategy is not as challenging as previously suggested (Finkel and Stump, 2007). Thus, SSA might be replaced with a less costly architecture while our model might be improved by conditioning on semantics and jointly decoding from a variable number of sources.

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³See *rex–regis*, *king* or *pax–pacis*, *peace*, which are technically conditioned on preceding vowel quality, though there are probably not enough training examples for the model to learn that.

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A Expanded Results

The figures in this appendix demonstrate the coverage after 1 and 2 sources for every language considered as well as their inter-predictability heat maps. Figures are enlarged to show all individual cells for the reader's convenience.



Figure 6: Coverage of Arabic target cells after SSA chooses the first two sources.

Arabic Noun Inter-Predictability

	SG DEF ACI	SG; DEF; GEN	SG; DEF; INFN	SG; DEF; NOM	SG; NDEF; ACC	SG; NDEF; GEN	SG; NDEF; INFM	SG; NDEF; NOM	SG; PSSD; ACC	SG; PSSD; GEN	SG; PSSD; INFM	SG; PSSD; NOM	DU; DEF; ACC	DU; DEF; GEN	DU; DEF; INFM	DU; DEF; NOM	DU; NDEF; ACC	DU; NDEF; GEN	DU; NDEF; INFM	DU; NDEF; NOM	DU; PSSD; ACC	DU; PSSD; GEN	DU; PSSD; INFM	DU; PSSD; NOM	PL; DEF; ACC	PL; DEF; GEN	PL; DEF; INFM	PL; DEF; NOM	PL; NDEF	PL; NDEF; GEN	N;PL; NDEF; INFM	PL; NDEF; NOM	PL; PSSD ; ACC	PL; PSSD; GEN	PL; PSSD; INFM	PL; PSSD; NOM	Av Predic	erage ctiveness
SG; DEF	; ACC 1.0	0.95	0.94	0.96	0.92	0.94	0.94	0.93	0.95	0.95	0.94	0.95	0.93	0.93	0.93	0.93	0.93	0.94	0.93	0.94	0.92	0.93	0.93	0.93	0.46								0.46	0.46		0.46		0.78
SG;DEF	; GEN 0.9	5 1.00	0.95	0.95	0.93	0.94	0.94	0.94	0.94	0.94	0.94	0.94	0.94	0.94	0.94	0.93	0.94	0.94	0.93	0.92	0.93	0.93	0.93	0.92	0.43											0.43		0.77
SG;DEF	INFM 0.9	5 0.94	1.00	0.95	0.93	0.94	0.94	0.93	0.95	0.95	0.95	0.95	0.92	0.92	0.92	0.92	0.93	0.93	0.93	0.93	0.93	0.94	0.94	0.93	0.45						0.46		0.46		0.46	0.45		0.78
SG;DEF	; NOM 0.9	5 0.95	0.95	1.00	0.93	0.94	0.95	0.94	0.95	0.95	0.95	0.95	0.93	0.93	0.93	0.91	0.93	0.93	0.94	0.92	0.94	0.94	0.94	0.93	0.42											0.42		0.77
SG;NDEF	; ACC 0.9	5 0.94	0.94	0.94	1.00	0.94	0.94	0.94	0.95	0.94	0.94	0.94	0.93	0.92	0.92	0.93	0.93	0.93	0.94	0.92	0.93	0.93	0.93	0.93	0.44											0.45		0.77
SG;NDEF	; GEN 0.9	5 0.94	0.94	0.94	0.94	1.00	0.95	0.95	0.95	0.95	0.95	0.95	0.92	0.91	0.91	0.91	0.93	0.93	0.93	0.93	0.93	0.93	0.93	0.93	0.44											0.44		0.77
SG;NDEF	INFM 0.9	5 0.95	0.95	0.95	0.93	0.94	1.00	0.94	0.95	0.95	0.95	0.95	0.92	0.93	0.92	0.92	0.92	0.93	0.93	0.92	0.92	0.92	0.92	0.92	0.48	0.49	0.48			0.49	0.49	0.48	0.48	0.49	0.48	0.47		0.78
SG;NDEF	; NOM 0.9	5 0.94	0.95	0.95	0.94	0.95	0.95	1.00	0.95	0.95	0.94	0.95	0.94	0.93	0.93	0.94	0.93	0.93	0.93	0.94	0.94	0.94	0.94	0.94	0.46						0.48	0.46	0.46	0.46		0.45		0.78
SG;PSSC	; ACC 0.9	5 0.94	0.95	0.94	0.93	0.93	0.94	0.93	1.00	0.94	0.94	0.94	0.94	0.93	0.94	0.93	0.94	0.94	0.94	0.93	0.94	0.94	0.93	0.93	0.44											0.44		0.77
SG;PSSC	; GEN 0.9	5 0.95	0.95	0.94	0.94	0.94	0.95	0.94	0.95	1.00	0.95	0.95	0.93	0.92	0.91	0.93	0.94	0.94	0.93	0.93	0.94	0.93	0.93	0.94	0.43											0.44		0.77
SG;PSSD	INFM 0.9	5 0.95	0.95	0.95	0.94	0.94	0.95	0.94	0.95	0.95	1.00	0.95	0.92	0.92	0.92	0.93	0.93	0.93	0.93	0.93	0.93	0.92	0.93	0.92	0.44						0.46					0.46		0.78
SG;PSSD	; NOM 0.9	5 0.95	0.95	0.95	0.93	0.94	0.95	0.94	0.95	0.94	0.95	1.00	0.93	0.93	0.92	0.93	0.94	0.95	0.94	0.94	0.94	0.94	0.94	0.93	0.42											0.43		0.77
DU;DEF	ACC 0.8	5 0.83	0.84	0.83	0.82	0.84	0.85	0.84	0.86	0.85	0.85	0.86	1.00	0.86	0.86	0.85	0.88	0.88	0.87	0.85	0.88	0.88	0.87	0.86	0.38											0.38		0.70
DU;DEF	; GEN 0.8	7 0.84	0.84	0.84	0.82	0.83	0.84	0.81	0.88	0.83	0.84	0.84	0.86	1.00	0.87	0.85	0.90	0.89	0.89	0.86	0.89	0.88	0.89	0.86	0.39											0.41		0.71
DU;DEF	INFM 0.8	8 0.88	0.87	0.87	0.86	0.85	0.87	0.85	0.88	0.86	0.86	0.86	0.88	0.87	1.00	0.88	0.88	0.88	0.88	0.88	0.89	0.88	0.88	0.87	0.38											0.38		0.71
DU;DEF	; NOM 0.8	8 0.85	0.84	0.85	0.83	0.84	0.84	0.84	0.87	0.85	0.84	0.85	0.90	0.89	0.90	1.00	0.90	0.89	0.90	0.89	0.90	0.90	0.90	0.89	0.42											0.41		0.72
DU;NDEF	; ACC 0.8	5 0.84	0.84	0.84	0.85	0.85	0.86	0.86	0.87	0.86	0.87	0.86	0.85	0.85	0.85	0.84	1.00	0.88	0.88	0.86	0.88	0.87	0.88	0.87	0.39											0.40		0.71
DU;NDEF	; GEN 0.8	0.84	0.84	0.84	0.83	0.85	0.86	0.84	0.85	0.85	0.85	0.85	0.85	0.86	0.86	0.85	0.88	1.00	0.88	0.87	0.88	0.88	0.88	0.87	0.36											0.38		0.70
DU;NDEF	INFM 0.8	0.80	0.81	0.81	0.83	0.84	0.84	0.83	0.85	0.83	0.84	0.83	0.85	0.85	0.85	0.84	0.87	0.86	1.00	0.85	0.87	0.86	0.86	0.85	0.37											0.38		0.69
DU;NDEF	; NOM 0.8	0.83	0.84	0.84	0.82	0.82	0.83	0.82	0.85	0.85	0.83	0.85	0.86	0.85	0.86	0.84	0.86	0.87	0.87	1.00	0.86	0.86	0.86	0.86	0.41											0.42		0.71
DU;PSSC	; ACC 0.8	0.84	0.83	0.83	0.84	0.85	0.86	0.85	0.86	0.85	0.85	0.86	0.86	0.85	0.86	0.85	0.88	0.88	0.88	0.87	1.00	0.88	0.88	0.87	0.38											0.39		0.70
DU;PSSD	; GEN 0.8	0.81	0.83	0.82	0.83	0.84	0.85	0.84	0.85	0.84	0.84	0.85	0.85	0.84	0.85	0.83	0.88	0.87	0.87	0.85	0.87	1.00	0.86	0.86	0.38											0.40		0.70
DU;PSSD	INFM 0.8	0.86	0.87	0.86	0.85	0.86	0.87	0.85	0.87	0.87	0.88	0.86	0.87	0.87	0.87	0.86	0.88	0.88	0.88	0.87	0.88	0.88	1.00	0.87	0.39											0.37		0.71
DU;PSSD	; NOM 0.8	0.85	0.85	0.86	0.84	0.85	0.85	0.84	0.87	0.85	0.85	0.85	0.88	0.88	0.88	0.88	0.89	0.89	0.89	0.88	0.89	0.89	0.89	1.00	0.37											0.37		0.71
PL;DEF	; ACC 0.3																								1.00	0.83	0.83	0.82	0.81	0.81	0.84	0.80	0.84	0.83	0.84	0.83		
PL;DEF	; GEN 0.0																								0.85	1.00	0.85	0.85	0.85	0.85	0.86	0.83	0.86	0.86	0.85	0.84		
PL;DEF	INFM 0.3																								0.86	0.85	1.00	0.85	0.83	0.84	0.85	0.83	0.85	0.86	0.85	0.85		
PL;DEF	NOM																								0.84	0.85	0.83	1.00	0.83	0.83	0.85	0.83	0.85	0.85	0.84	0.85		
PL;NDEF	ACC																								0.82	0.81	0.81	0.80	1.00	0.83	0.84	0.81	0.84	0.83	0.83	0.83		
PL;NDEF	; GEN 0.4																								0.81	0.80	0.80	0.81	0.82	1.00	0.83	0.82	0.83	0.82	0.83	0.82		
PL;NDEF	INFM																								0.82	0.82	0.82	0.82	0.83	0.82	1.00	0.82	0.82	0.82	0.84	0.84		
PL;NDEF	; NOM 0.3																								0.83	0.83	0.82	0.83	0.82	0.83	0.83	1.00	0.84	0.84	0.84	0.83		
PL;PSSC	; ACC 0.4																								0.83	0.83	0.82	0.83	0.83	0.83	0.84	0.83	1.00	0.83	0.83	0.85		
PL;PSSC	; GEN																								0.81	0.83	0.84	0.83	0.78	0.82	0.84	0.81	0.81	1.00	0.85	0.83		
PL;PSSD	INFM																								0.84	0.84	0.85	0.85	0.79	0.81	0.85	0.82	0.84	0.85	1.00	0.85		
PL;PSSD	NOM																								0.85	0.82	0.84	0.85	0.85	0.83	0.86	0.84	0.86	0.85	0.86	1.00		
																																					_	
Avera Predictabi	ge lity 0.7	0.72	0.72	0.72	0.72	0.72	0.73	0.72	0.73	0.73	0.73	0.73	0.73	0.73	0.73	0.72	0.74	0.74	0.74	0.73	0.74	0.74	0.74	0.73												0.56		

Figure 7: Inter-predictability heat map of Arabic cells.



Figure 8: Coverage of German target cells after SSA chooses the first two sources.

German Verb Inter-Predictability

	NFIN	IMP; 2;PL	IMP; 2;SG	IND; PRS; 1;SG	IND; PRS; 2;SG	IND; PRS; 3;SG	SBJV; PRS; 1;SG	SBJV; PRS; 2;SG	SBJV; PRS; 3;SG	IND; PRS; 1;PL	IND; PRS; 2;PL	IND; PRS; 3;PL	SBJV; PRS; 1;PL	SBJV; PRS; 2;PL	SBJV; PRS; 3;PL	IND; PST; 1;SG	IND; PST; 2;SG	IND; PST; 3;SG	SBJV; PST; 1;SG	SBJV; PST; 2;SG	SBJV; PST; 3;SG	IND; PST; 1;PL	IND; PST; 2;PL	IND; PST; 3;PL	SBJV; PST; 1;PL	SBJV; PST; 2;PL	SBJV; PST; 3;PL	Average Predictiveness
NFIN	1.00	0.82	0.78	0.83	0.77	0.77	0.84	0.83	0.84	0.83	0.82	0.83	0.83	0.83	0.83												0.71	
IMP;2;PL	0.87	1.00	0.87	0.91	0.86	0.87	0.93	0.93	0.92	0.92	0.92	0.92	0.92	0.92	0.92	0.79	0.78	0.79	0.79	0.79	0.79	0.78	0.78	0.78	0.79	0.79	0.79	0.86
IMP;2;SG	0.81	0.87	1.00	0.87	0.87	0.87	0.88	0.87	0.88	0.87	0.87	0.87	0.87	0.87	0.87					0.76					0.76	0.76	0.76	0.82
IND;PRS;1; SG	0.86	0.89	0.85	1.00	0.79	0.82	0.91	0.91	0.91	0.91	0.89	0.91	0.91	0.91	0.91				0.76						0.76		0.76	0.83
IND;PRS;2; SG	0.80	0.85	0.84	0.83	1.00	0.90	0.85	0.86	0.85	0.84	0.85	0.84	0.84	0.85	0.84	0.77	0.77	0.77	0.76	0.77		0.78	0.77	0.77	0.77	0.76	0.77	0.82
IND;PRS;3; SG	0.82	0.88	0.87	0.86	0.90	1.00	0.87	0.87	0.87	0.86	0.87	0.86	0.86	0.88	0.86	0.77	0.76	0.77	0.77	0.77	0.77	0.78	0.77	0.78	0.78	0.77	0.78	0.83
SBJV;PRS;1; SG	0.84	0.90	0.82	0.88	0.82	0.83	1.00	0.90	0.91	0.89	0.90	0.89	0.89	0.91	0.89				0.77	0.77	0.77				0.77	0.77	0.77	0.83
SBJV;PRS;2; SG	0.87	0.90	0.85	0.89	0.84	0.83	0.91	1.00	0.91	0.90	0.89	0.90	0.90	0.91	0.90	0.77	0.76	0.77	0.78	0.77	0.78	0.77	0.76	0.77	0.78	0.77	0.78	0.84
SBJV;PRS;3; SG	0.84	0.88	0.83	0.87	0.81	0.81	0.89	0.89	1.00	0.89	0.88	0.89	0.89	0.90	0.89												0.75	0.82
IND;PRS;1; PL	0.86	0.89	0.85	0.89	0.82	0.83	0.91	0.91	0.91	1.00	0.89	0.91	0.91	0.91	0.91				0.76	0.76	0.77				0.76	0.77	0.77	0.83
IND;PRS;2; PL	0.86	0.92	0.85	0.90	0.83	0.84	0.92	0.91	0.91	0.90	1.00	0.90	0.91	0.92	0.90	0.79	0.78	0.79	0.78	0.78	0.78	0.78	0.78	0.78	0.78	0.78	0.78	0.85
IND;PRS;3; PL	0.88	0.90	0.86	0.90	0.82	0.83	0.92	0.92	0.92	0.92	0.90	1.00	0.92	0.92	0.92	0.77	0.76	0.77	0.78	0.78	0.78	0.78	0.77	0.77	0.78	0.79	0.78	0.85
SBJV;PRS;1; PL	0.88	0.90	0.85	0.90	0.82	0.84	0.92	0.92	0.92	0.92	0.90	0.92	1.00	0.92	0.92	0.77	0.77	0.77	0.77	0.77	0.77	0.77	0.77	0.77	0.77	0.77	0.77	0.84
SBJV;PRS;2; PL	0.86	0.90	0.83	0.88	0.83	0.84	0.91	0.91	0.91	0.90	0.90	0.89	0.90	1.00	0.90												0.75	0.82
SBJV;PRS;3; PL	0.85	0.89	0.84	0.88	0.81	0.82	0.90	0.90	0.90	0.90	0.89	0.90	0.90	0.89	1.00												0.74	0.82
IND;PST;1; SG	0.79	0.83	0.81	0.83	0.83	0.83	0.84	0.84	0.84	0.83	0.83	0.83	0.83	0.84	0.83	1.00	0.90	0.90	0.89	0.89	0.89	0.91	0.90	0.91	0.90	0.90	0.90	0.86
IND;PST;2; SG	0.80	0.84	0.80	0.81	0.73	0.83	0.84	0.84	0.85	0.84	0.83	0.84	0.84	0.84	0.84	0.89	1.00	0.90	0.90	0.90	0.90	0.91	0.91	0.91	0.90	0.90	0.90	0.86
IND;PST;3; SG	0.78	0.84	0.82	0.82	0.83	0.83	0.84	0.84	0.83	0.83	0.84	0.83	0.83	0.84	0.83	0.90	0.90	1.00	0.89	0.89	0.89	0.90	0.90	0.90	0.89	0.89	0.89	0.86
SBJV;PST;1; SG	0.77	0.84	0.83	0.82	0.81	0.82	0.84	0.83	0.84	0.83	0.84	0.83	0.83	0.84	0.83	0.88	0.88	0.89	1.00	0.91	0.92	0.90	0.90	0.90	0.92	0.92	0.92	0.86
SBJV;PST;2;	0.76	0.83	0.79	0.81	0.81	0.81	0.82	0.83	0.83	0.82	0.83	0.82	0.82	0.83	0.82	0.88	0.88	0.88	0.91	1.00	0.90	0.89	0.89	0.89	0.91	0.91	0.91	0.85
SBJV;PST;3; SG	0.80	0.84	0.81	0.83	0.81	0.83	0.85	0.84	0.85	0.84	0.84	0.84	0.84	0.85	0.84	0.89	0.90	0.89	0.92	0.92	1.00	0.90	0.90	0.90	0.92	0.92	0.92	0.87
IND;PST;1; PL	0.79	0.85	0.81	0.81	0.84	0.84	0.84	0.84	0.84	0.83	0.84	0.83	0.83	0.84	0.83	0.92	0.93	0.92	0.92	0.91	0.92	1.00	0.94	0.94	0.92	0.92	0.91	0.87
IND;PST;2; PL	0.76	0.83	0.79	0.79	0.81	0.83	0.82	0.82	0.82	0.81	0.82	0.81	0.81	0.82	0.81	0.88	0.90	0.88	0.88	0.88	0.88	0.90	1.00	0.90	0.88	0.88	0.88	0.85
IND;PST;3; PL	0.78	0.83	0.81	0.82	0.82	0.83	0.84	0.83	0.84	0.82	0.83	0.83	0.82	0.84	0.83	0.89	0.90	0.89	0.88	0.88	0.88	0.91	0.91	1.00	0.88	0.88	0.88	0.86
SBJV;PST;1; PL	0.81	0.85	0.81	0.82	0.82	0.84	0.85	0.84	0.85	0.83	0.84	0.83	0.83	0.85	0.83	0.89	0.89	0.90	0.92	0.91	0.92	0.90	0.91	0.91	1.00	0.92	0.92	0.87
SBJV;PST;2;	0.78	0.83	0.79	0.80	0.81	0.82	0.82	0.83	0.83	0.81	0.82	0.81	0.81	0.82	0.82	0.86	0.87	0.87	0.89	0.89	0.89	0.87	0.87	0.87	0.89	1.00	0.89	0.85
SBJV;PST;3;	0.81	0.86	0.83	0.83	0.83	0.85	0.85	0.86	0.85	0.84	0.86	0.84	0.84	0.86	0.84	0.88	0.89	0.88	0.92	0.92	0.92	0.90	0.90	0.90	0.91	0.92	1.00	0.87
Average Predictability	0.83	0.87	0.83	0.85	0.83	0.84	0.87	0.87	0.88	0.87	0.87	0.87	0.87	0.87	0.87			0.82	0.83	0.83	0.83	0.82	0.82	0.83	0.83	0.83	0.83	

Figure 9: Inter-predictability heat map of German cells.



Figure 10: Coverage of English target cells after SSA chooses the first two sources.



English Verb Inter-Predictability



Figure 11: Inter-predictability heat map of English cells.



Figure 12: Coverage of Russian target cells after SSA chooses the first two sources.

	NOM; SG	GEN; SG	DAT; SG	ACC; SG	ESS; SG	INS; SG	NOM; PL	GEN; PL	DAT; PL	ACC; PL	ESS; PL	INS; PL	A Pre	verage) iess
NOM;SG	1.00	0.94	0.95	0.87	0.95	0.93	0.95	0.93	0.96	0.81	0.96	0.96		0.93	
GEN;SG	0.91	1.00	0.96	0.82	0.96	0.94	0.95	0.92	0.97	0.80	0.97	0.97		0.93	
DAT;SG	0.92	0.96	1.00	0.82	0.97	0.94	0.94	0.92	0.96	0.77	0.96	0.96		0.93	
ACC;SG	0.97	0.95	0.95	1.00	0.95	0.93	0.95	0.93	0.97	0.93	0.96	0.96		0.96	
ESS;SG	0.76	0.77	0.79		1.00	0.78	0.91	0.76	0.94	0.77	0.95	0.95			
INS;SG	0.93	0.97	0.97	0.82	0.97	1.00	0.94	0.92	0.96	0.80	0.97	0.97		0.94	
NOM;PL	0.78	0.81	0.81		0.96	0.79	1.00	0.80	0.99	0.82	0.99	0.99		0.87	
GEN;PL	0.90	0.90	0.90	0.77	0.92	0.90	0.92	1.00	0.95	0.78	0.95	0.95		0.90	
DAT;PL	0.76	0.78	0.77		0.94	0.76	0.94	0.78	1.00	0.78	0.98	0.97			
ACC;PL	0.79	0.82	0.81	0.80	0.94	0.80	0.95	0.79	0.96	1.00	0.96	0.96		0.88	
ESS;PL	0.78	0.79	0.78		0.95	0.76	0.94	0.78	0.98	0.79	1.00	0.99			
INS;PL	0.78	0.79	0.78		0.95	0.77	0.94	0.79	0.98	0.78	0.98	1.00			
Average Predictability	0.86	0.87	0.87		0.96	0.86	0.94	0.86	0.97	0.82	0.97	0.97			

Russian Noun Inter-Predictability

Figure 13: Inter-predictability heat map of Russian cells.



Figure 14: Coverage of Latin target cells after SSA chooses the first two sources.

														•
	NOM; SG	GEN; SG	DAT; SG	ACC; SG	ABL; SG	VOC; SG	NOM; PL	GEN; PL	DAT; PL	ACC; PL	ABL; PL	VOC; PL	Pre	Average edictiveness
NOM; SG	1.00	0.81	0.80	0.79	0.81	0.87	0.81	0.80	0.80	0.78	0.81	0.82		0.82
GEN; SG	0.75	1.00	0.93	0.87	0.92	0.77	0.82	0.89	0.93	0.82	0.93	0.84		0.87
DAT; SG	0.72	0.89	1.00	0.85	0.90	0.73	0.80	0.86	0.92	0.79	0.91	0.82		0.85
ACC; SG	0.70	0.85	0.85	1.00	0.87	0.71	0.78	0.83	0.87	0.78	0.88	0.82		0.83
ABL; SG	0.77	0.93	0.93	0.88	1.00	0.77	0.84	0.89	0.92	0.84	0.92	0.84		0.88
VOC; SG	0.89	0.83	0.83	0.82	0.82	1.00	0.83	0.83	0.85	0.82	0.85	0.83		0.85
NOM; PL	0.83	0.89	0.89	0.85	0.90	0.82	1.00	0.85	0.91	0.90	0.90	0.93		0.89
GEN; PL	0.71	0.86	0.87	0.81	0.85	0.72	0.77	1.00	0.88	0.77	0.88	0.78		0.82
DAT; PL		0.66	0.68	0.63	0.69	0.58			1.00	0.64	0.90	0.65		
ACC; PL	0.80	0.88	0.89	0.87	0.91	0.82	0.86	0.85	0.90	1.00	0.90	0.95		0.88
ABL; PL	0.57	0.70	0.70	0.65	0.68	0.57	0.64	0.68	0.91	0.65	1.00	0.65		
VOC; PL	0.81	0.90	0.91	0.89	0.90	0.81	0.93	0.87	0.91	0.94	0.91	1.00		0.90
Average Predictability		0.85	0.86	0.83	0.85	0.76	0.81	0.83	0.90	0.81	0.90	0.83		

Latin Noun Inter-Predictability

Figure 15: Inter-predictability heat map of Latin cells.



Figure 16: Coverage of Hungarian target cells after SSA chooses the first two sources.

Hungarian Noun Inter-Predictability

	NOM; SG	ACC; SG	DAT; SG	AT+ ABL; SG	AT+ ALL; SG	AT+ ESS; SG	FRML; SG	IN+ ABL; SG	IN+ ALL; SG	IN+ ESS; SG	INST; SG	ON+ ABL; SG	ON+ ALL; SG	ON+ ESS; SG	PRP; SG	TERM; SG	TRANS; SG	NOM; PL	ACC; PL	DAT; PL	AT+ ABL; PL	AT+ ALL; PL	AT+ ESS; PL	FRML; PL	IN+ ABL; PL	IN+ ALL; PL	IN+ ESS; PL	INST; PL	ON+ ABL; PL	ON+ ALL; PL	ON+ ESS; PL	PRP; PL	TERM; PL	IRANS; PL	Average Predictiveness
NOM;SG	1.00	0.81	0.95	0.96	0.94	0.95	0.97	0.95	0.96	0.95	0.94	0.96	0.95	0.94	0.97	0.97	0.94	0.82	0.82	0.83	0.83	0.83	0.82	0.82	0.83	0.82	0.83	0.83	0.83	0.82	0.83	0.83	0.83	0.82	0.89
ACC;SG	0.94	1.00	0.93	0.93	0.92	0.93	0.94	0.93	0.93	0.93	0.90	0.93	0.93	0.94	0.94	0.94	0.91	0.93	0.93	0.93	0.92	0.93	0.93	0.93	0.93	0.93	0.93	0.92	0.93	0.93	0.92	0.93	0.93	0.93	0.93
DAT;SG	0.95		1.00	0.96	0.95	0.96	0.95	0.95	0.95	0.95	0.92	0.95	0.95	0.94	0.95	0.96	0.92	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.89
AT+ABL;SG	0.89		0.93	1.00	0.91	0.93	0.90	0.93	0.93	0.93	0.88	0.93	0.93	0.89	0.92	0.92	0.89		0.81	0.81	0.81	0.81	0.81	0.82	0.81	0.81	0.81	0.81	0.82	0.81	0.81	0.81	0.81		C 38
AT+ALL;SG	0.93		0.95	0.95	1.00	0.96	0.94	0.95	0.95	0.95	0.93	0.95	0.95	0.93	0.95	0.93	0.91	0.82	0.81	0.82	0.82	0.82	0.82	0.82	0.82	0.82	0.83	0.83	0.83	0.83	0.82	0.82	0.83	0.83	0.88
AT+ESS;SG	0.95		0.97	0.96	0.95	1.00	0.95	0.96	0.96	0.97	0.92	0.97	0.97	0.94	0.96	0.94	0.91	0.83	0.83	0.83	0.82	0.83	0.84	0.82	0.83	0.83	0.83	0.82	0.83	0.83	0.82	0.83	0.82	0.83	0.89
FRML;SG	0.96	0.81	0.94	0.94	0.94	0.94	1.00	0.94	0.94	0.94	0.93	0.94	0.94	0.93	0.95	0.95	0.93	0.83	0.83	0.83	0.83	0.83	0.83	0.84	0.83	0.83	0.83	0.83	0.83	0.83	0.83	0.83	0.83	0.83	0.88
IN+ABL;SG	0.95	0.81	0.96	0.95	0.94	0.95	0.95	1.00	0.96	0.96	0.94	0.95	0.95	0.93	0.95	0.95	0.94	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.89
IN+ALL;SG	0.96	0.83	0.97	0.97	0.96	0.97	0.96	0.98	1.00	0.97	0.96	0.97	0.97	0.95	0.97	0.97	0.96	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.90
IN+ESS;SG	0.96	0.81	0.96	0.96	0.95	0.96	0.96	0.96	0.96	1.00	0.94	0.96	0.96	0.93	0.96	0.96	0.94	0.84	0.83	0.84	0.83	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.84	0.83	0.83	0.84	0.84	0.83	0.89
INST;SG	0.91		0.92	0.94	0.91	0.92	0.91	0.92	0.92	0.92	1.00	0.92	0.92	0.90	0.92	0.92	0.91							0.80		0.80							0.80		
ON+ABL;SG	0.96	0.83	0.96	0.96	0.94	0.96	0.96	0.96	0.96	0.96	0.93	1.00	0.96	0.93	0.96	0.96	0.93	0.85	0.84	0.84	0.85	0.84	0.84	0.84	0.84	0.84	0.84	0.85	0.84	0.84	0.84	0.84	0.84	0.84	0.90
ON+ALL;SG	0.94	0.82	0.95	0.94	0.94	0.95	0.94	0.95	0.95	0.95	0.91	0.95	1.00	0.92	0.94	0.93	0.92	0.83	0.83	0.83	0.83	0.83	0.83	0.84	0.84	0.84	0.84	0.83	0.83	0.84	0.83	0.83	0.84	0.83	0.88
ON+ESS;SG	0.94	0.82	0.94	0.94	0.93	0.94	0.94	0.94	0.94	0.94	0.89	0.94	0.94	1.00	0.94	0.94	0.90	0.85	0.85	0.85	0.85	0.85	0.85	0.85	0.85	0.85	0.85	0.85	0.85	0.85	0.84	0.85	0.85	0.84	0.89
PRP;SG	0.94	0.80	0.94	0.93	0.93	0.94	0.94	0.94	0.93	0.94	0.93	0.94	0.94	0.92	1.00	0.95	0.92	0.83	0.82	0.83	0.82	0.83	0.82	0.83	0.83	0.83	0.83	0.83	0.83	0.83	0.83	0.82	0.83	0.83	0.88
TERM;SG	0.94	0.81	0.93	0.93	0.93	0.94	0.95	0.93	0.93	0.93	0.91	0.93	0.93	0.92	0.95	1.00	0.91	0.82	0.81	0.81	0.82	0.82	0.82	0.82	0.82	0.82	0.82	0.82	0.81	0.81	0.81	0.82	0.82	0.81	0.87
TRANS;SG	0.91	0.81	0.92	0.94	0.89	0.92	0.92	0.93	0.93	0.93	0.93	0.92	0.92	0.90	0.92	0.92	1.00	0.81	0.81	0.82	0.82	0.82	0.81	0.82	0.82	0.82	0.81	0.82	0.82	0.82	0.82	0.81	0.82	0.82	0.87
NOM;PL	0.92	0.90	0.93	0.93	0.92	0.93	0.92	0.93	0.93	0.93	0.89	0.93	0.93	0.94	0.93	0.93	0.89	1.00	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.94
ACC;PL	0.95	0.92	0.95	0.95	0.95	0.95	0.94	0.95	0.95	0.95	0.93	0.95	0.95	0.96	0.95	0.95	0.92	0.97	1.00	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.96
DAT;PL	0.93	0.88	0.93	0.93	0.93	0.94	0.93	0.94	0.94	0.94	0.92	0.94	0.94	0.95	0.94	0.94	0.92	0.97	0.97	1.00	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.95
AT+ABL;PL	0.95	0.91	0.95	0.94	0.94	0.94	0.95	0.95	0.95	0.95	0.93	0.95	0.95	0.96	0.95	0.95	0.93	0.98	0.98	0.98	1.00	0.97	0.98	0.98	0.98	0.98	0.98	0.98	0.97	0.98	0.98	0.98	0.98	0.98	0.96
AT+ALL;PL	0.89	0.84	0.91	0.90	0.89	0.91	0.90	0.91	0.91	0.91	0.84	0.91	0.91	0.90	0.91	0.91	0.80	0.94	0.95	0.94	0.95	1.00	0.95	0.94	0.95	0.94	0.94	0.94	0.94	0.94	0.94	0.95	0.94	0.94	0.92
AT+ESS;PL	0.93	0.89	0.93	0.93	0.92	0.93	0.91	0.93	0.93	0.93	0.91	0.93	0.93	0.94	0.93	0.93	0.91	0.96	0.96	0.96	0.96	0.96	1.00	0.96	0.96	0.96	0.96	0.96	0.97	0.96	0.96	0.96	0.96	0.96	0.94
FRML;PL	0.94	0.91	0.95	0.94	0.94	0.95	0.94	0.94	0.94	0.94	0.93	0.95	0.95	0.95	0.94	0.94	0.93	0.97	0.97	0.97	0.97	0.97	0.97	1.00	0.97	0.97	0.97	0.97	0.97	0.97	0.96	0.97	0.97	0.97	0.96
IN+ABL;PL	0.93	0.90	0.94	0.93	0.92	0.94	0.93	0.93	0.94	0.94	0.91	0.94	0.94	0.94	0.94	0.94	0.91	0.96	0.96	0.96	0.96	0.96	0.96	0.96	1.00	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.95
IN+ALL;PL	0.94	0.92	0.95	0.93	0.94	0.95	0.94	0.94	0.95	0.94	0.93	0.95	0.95	0.95	0.94	0.94	0.92	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	1.00	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.96
IN+ESS;PL	0.94	0.90	0.95	0.95	0.93	0.95	0.94	0.95	0.95	0.95	0.92	0.95	0.95	0.95	0.94	0.95	0.92	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	1.00	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.95
INST;PL	0.95	0.91	0.95	0.95	0.95	0.95	0.94	0.95	0.95	0.95	0.92	0.95	0.95	0.95	0.94	0.95	0.92	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	1.00	0.97	0.97	0.97	0.97	0.97	0.96	0.96
ON+ABL;PL	0.93	0.90	0.94	0.93	0.93	0.94	0.93	0.94	0.94	0.94	0.90	0.94	0.94	0.94	0.94	0.94	0.89	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	1.00	0.96	0.96	0.97	0.96	0.96	0.95
ON+ALL;PL	0.94	0.92	0.94	0.94	0.93	0.94	0.94	0.95	0.94	0.94	0.92	0.94	0.94	0.96	0.94	0.94	0.91	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.97	0.98	0.97	0.97	0.97	1.00	0.97	0.97	0.97	0.97	0.95
ON+ESS;PL	0.93	0.89	0.93	0.92	0.91	0.93	0.92	0.93	0.93	0.93	0.88	0.93	0.93	0.93	0.93	0.92	0.88	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.96	0.97	0.96	0.96	0.96	0.96	1.00	0.96	0.96	0.96	0.94
PRP;PL	0.94	0.90	0.94	0.94	0.93	0.94	0.93	0.94	0.94	0.94	0.91	0.95	0.94	0.95	0.95	0.94	0.90	0.97	0.97	0.97	0.97	0.96	0.97	0.97	0.97	0.97	0.97	0.96	0.97	0.97	0.96	1.00	0.97	0.97	0.95
TERM;PL	0.94	0.90	0.94	0.93	0.93	0.94	0.94	0.94	0.94	0.94	0.90	0.94	0.94	0.94	0.94	0.94	0.89	0.97	0.97	0.96	0.96	0.96	0.96	0.97	0.97	0.97	0.96	0.96	0.96	0.97	0.96	0.97	1.00	0.96	0.95
TRANS;PL	0.93	0.90	0.94	0.93	0.92	0.93	0.93	0.93	0.93	0.93	0.89	0.93	0.94	0.93	0.93	0.94	0.89	0.97	0.96	0.97	0.96	0.96	0.96	0.97	0.97	0.97	0.97	0.96	0.96	0.97	0.96	0.97	0.96	1.00	0.95
Average Predictability	0.94		0.94	0.94	0.93	0.94	0.94	0.94	0.94	0.94	0.92	0.94	0.94	0.94	0.94	0.94	0.91	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	0.90	

Figure 17: Inter-pre	dictability heat mar	o of Hung	arian cells	5.
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Figure 18: Coverage of Irish target cells after SSA chooses the first two sources.

	NOM; SG	NOM; SG; DEF	GEN; SG	GEN; SG; DEF	DAT; SG	DAT; SG; DEF	VOC; SG	NOM; PL	NOM; PL; DEF	GEN; PL	DAT; PL	DAT; PL; DEF	VOC; PL	Average Predictiveness
NOM;SG	1.00	0.36			0.50	0.44	0.42							0.32
NOM;SG; DEF	0.51	1.00	0.28		0.50	0.47	0.40							0.34
GEN;SG	0.33	0.21	1.00		0.32		0.29							
GEN;SG; DEF	0.29		0.25	1.00	0.28		0.27	0.43	0.44	0.44	0.43	0.46	0.45	0.40
DAT;SG	0.54	0.38	0.34	0.14	1.00	0.51	0.44							0.35
DAT;SG; DEF	0.59	0.44	0.31		0.58	1.00	0.45							0.37
VOC;SG	0.39		0.29		0.37	0.35	1.00	0.21						0.30
NOM;PL	0.32		0.29	0.41	0.28			1.00	0.48	0.40	0.49	0.49	0.45	0.41
NOM;PL; DEF	0.32		0.32	0.42	0.32			0.50	1.00	0.41	0.50	0.51	0.47	0.43
GEN;PL	0.27		0.27	0.40		0.27		0.41	0.38	1.00	0.41	0.38	0.43	0.38
DAT;PL	0.31		0.29	0.38	0.29	0.27	0.27	0.48	0.50	0.38	1.00	0.47	0.42	0.40
DAT;PL; DEF	0.28		0.28	0.41	0.27	0.27	0.28	0.49	0.53	0.42	0.48	1.00	0.45	0.41
VOC;PL	0.22			0.29				0.33	0.32	0.35	0.34	0.33	1.00	0.32
Average Predictability	0.41		0.33	0.32	0.40	0.37	0.37	0.37	0.37	0.35	0.37	0.37	0.38	

Irish Noun Inter-Predictability

Figure 19: Inter-predictability heat map of Irish cells.